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## A3 Test 1

## Multiple Choice

Identify the choice that best completes the statement or answers the question.
$\qquad$ 1. Solve $-4(24+8 y)=-64$.
a. $y=4$
b. $y=-11$
c. $y=-1$
d. $y=5$
$\qquad$ 2. Solve $3 n-24=14-30 n$.
a. $n=2$
b. $n=1 \frac{5}{33}$
c. $n=1 \frac{11}{27}$
d. $n=\frac{10}{33}$
$\qquad$ 3. Solve $5 j-12+13 j=-4+18 j-8$.
a. The solution set is all real numbers, or $\mathbb{R}$.
b. The solution set is the empty set.
c. $j=-12$
d. $j=0$
$\qquad$ 4. Solve and graph $-2 a-7>-3$.
a. $\quad a<-2$

b. $\quad a>-2$

c. $\quad a>5$

d. $a<5$

5. Solve and graph $5(-4+2 x) \geq 2(5 x+4)$.
a. $x \geq-\frac{3}{5}$

b. The inequality has no solution. The solution set is the empty set.

c. The solution set is the set of all real numbers.

d. $x \geq \frac{7}{5}$

6. Solve the equation $9|x-4|=81$.
a. $x=13$
b. $\quad x=85$ or $x=-77$
c. $x=13$ or $x=-5$
d. $x=85$
$\qquad$ 7. Solve the inequality $|12+4 x|>16$ and graph the solution set.
a. $(-\infty, \infty)$

c. $(-\infty,-7) \cup(1, \infty)$

b. $(-7,1)$
d. $(1, \infty)$

$\qquad$
8. Solve $\frac{|x-12|}{4} \leq 1$ and graph the solution set.
a. $-16 \leq x \leq 16$
c. $8 \leq x$ and $16 \leq x$

b. $8 \geq x$ and $16 \leq x$
No solution.
d. $8 \leq x \leq 16$

9. Solve the inequality and graph the solution set for $-6|6+3 x|=-24$.
a. No solution.
c. $x=-\frac{2}{3}$

b. $\quad x=-\frac{2}{3}$ or $x=-\frac{10}{3}$
d. $x=-10$ or $x=6$

10. Solve $-2(-16+4 y)=24$.
a. $y=-2$
b. $\quad y=10$
c. $y=1$
d. $\quad y=-7$
11. Solve $2(24-6 y)=-48$.
a. $y=0$
b. $y=12$
c. $y=16$
d. $y=8$
12. Solve $5 p+4=26+6 p$.
a. $\quad p=30$
b. $\quad p=-21$
c. $p=-2$
d. $p=-22$
13. Solve $7 k+19=6+19 k$.
a. $k=1 \frac{1}{12}$
b. $k=2 \frac{1}{12}$
c. $k=2$
d. $k=\frac{1}{2}$
14. Solve and graph $-8 t+12>-4$.
a. $t<2$

b. $t>2$

c. $t<-1$

d. $t>-1$

15. Solve and graph $t-6 \leq-1$.
a. $t \geq 5$

b. $t \leq 5$

c. $t \leq-7$

d. $t \geq-7$

16. Solve and graph $3(6-4 x)<-4(3 x-6)$.
a. The solution set is the set of all real numbers.

b. The inequality has no solution. The solution set is the empty set.

c. $\quad x>-\frac{7}{4}$

d. $\quad x>-\frac{1}{4}$

17. Solve and graph $6(3+4 x)<4(6 x-2)$.
a. $x<\frac{5}{24}$

b. $x<-\frac{13}{24}$

c. The solution set is the set of all real numbers.

d. The inequality has no solution. The solution set is the empty set.

18. Solve the equation $5|x+4|=15$.
a. $\quad x=-1$ or $x=-7$
b. $x=11$
c. $x=11$ or $x=-19$
d. $x=-1$
19. Solve the equation $9|x-7|=45$.
a. $x=12$ or $x=2$
b. $x=52$ or $x=-38$
c. $x=12$
d. $x=52$
20. Solve $\frac{|x-8|}{2} \leq 4$ and graph the solution set.
a. $-16 \leq x \leq 16$

b. $0 \leq x \leq 16$

c. $0 \leq x$ and $16 \leq x$

d. $0 \geq x$ and $16 \leq x$

No solution.
21. Solve $\frac{|x-14|}{3} \leq 5$ and graph the solution set.
a. $-1 \leq x \leq 29$
c. $-29 \leq x \leq 29$

b. $\quad-1 \geq x$ and $29 \leq x$
d. $-1 \leq x$ and $29 \leq x$
No solution.

22. Solve the inequality and graph the solution set for $-2|2+10 x|=-25$.
a. $\quad x=\frac{21}{20}$ or $x=-\frac{29}{20}$

c. $\quad x=-\frac{27}{10}$ or $x=\frac{23}{10}$

b. $x=\frac{21}{20}$
d. No solution.

23. Solve the inequality and graph the solution set for $-3|2+6 x|=-24$.
a. No solution.
c. $x=-\frac{13}{3}$ or $x=\frac{11}{3}$

b. $\quad x=1$ or $x=-\frac{5}{3}$

d. $x=1$

24. Solve the inequality $|6+3 x|>15$ and graph the solution set.
a. $(3, \infty)$
c. $(-\infty,-7) \cup(3, \infty)$

b. $(-7,3)$
d. $(-\infty, \infty)$


## A3 Test 1

Answer Section

## MULTIPLE CHOICE

1. ANS: C

$$
\begin{aligned}
-4(24+8 y) & =-64 & & \\
-96-32 y & =-64 & & \text { Distribute }-4 . \\
-32 y & =32 & & \text { Add } 96 \text { to both sides. } \\
y & =-1 & & \text { Divide by }-32 .
\end{aligned}
$$

REF: Page 91 OBJ: 2-1.2 Solving Equations with the Distributive Property
2. ANS: B

First, collect all variable terms on one side and all constant terms on the other side. Then, isolate the variable.
REF: Page 92 OBJ: 2-1.3 Solving Equations with Variables on Both Sides
3. ANS: A
$5 j-12+13 j=-4+18 j-8$
$18 j-12=18 j-12 \quad$ Simplify.
$\frac{-18 j}{-12=-12}$
Identity. The solution set is all real numbers.

REF: Page 92 OBJ: 2-1.4 Identifying Identities and Contradictions
4. ANS: A

To isolate the variable, first undo the addition or subtraction. Then, undo the multiplication by dividing each side of the inequality by the coefficient of the variable. If the coefficient is negative, reverse the inequality symbol. Next, graph the solution.

Remember, a " $>$ " or " $<$ " graph has an open circle at that value. A " $\geq$ " or " $\leq$ " graph has a closed circle at that value.

A " $>$ " or " 2 " graph has an arrow to the right, and a " $<$ " or " $\leq$ " graph has an arrow to the left.
REF: Page 93 OBJ: 2-1.5 Solving Inequalities
5. ANS: B
$5(-4+2 x) \geq 2(5 x+4)$
$-20+10 x \geq 10 x+8 \quad$ Use the Distributive Property.
$0 x \geq 28 \quad$ Isolate $x$. Then simplify.
$0 \geq 28$
Contradiction.
The inequality has no solution. The solution set is the empty set.

6. ANS: C
$9|x-4|=81$
$|x-4|=9 \quad$ Isolate the absolute-value expression by dividing both sides by 9 .
$x-4=9$ or $x-4=-9 \quad$ Rewrite the absolute value as a disjunction.
$x=13$ or $x=-5 \quad$ Add 4 to both sides of each equation.

REF: Page 152 OBJ: 2-8.2 Solving Absolute-Value Equations
7. ANS: C

Rewrite the absolute value as a disjunction. Then subtract 12 from both sides and divide by 4 .

$$
\begin{array}{ccc}
|12+4 x|>16 & & \\
12+4 x>16 & \text { or } & 12+4 x<-16 \\
4 x>4 & \text { or } & 4 x<-28 \\
x>1 & \text { or } & x<-7
\end{array}
$$

REF: Page 152 OBJ: 2-8.3 Solving Absolute-Value Inequalities with Disjunctions
8. ANS: D
$\frac{|x-12|}{4} \leq 1 \quad$ Multiply both sides by 4.
$|x-12| \leq 4 \quad$ Rewrite the absolute value as a conjunction.
$x-12 \leq 4$ and $x-12 \geq-4 \quad$ Simplify.
$x \leq 16$ and $x \geq 8$
Graph the solution on a number line. As the inequality symbols include equality, circles should be filled in at the limits indicated by each expression. "Greater than" means values larger than a limit will be included. "Less than" indicates values less than the limit will be included. If there are no solutions that satisfy both inequalities, there is no solution. If all values satisfy the requirements, the solution includes all real umbers.

REF: Page 153 OBJ: 2-8.4 Solving Absolute-Value Inequalities with Conjunctions
9. ANS: B

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10. ANS: C

$$
\begin{aligned}
-2(-16+4 y) & =24 & & \\
32-8 y & =24 & & \text { Distribute }-2 . \\
-8 y & =-8 & & \text { Add }-32 \text { to both sides. } \\
y & =1 & & \text { Divide by }-8 .
\end{aligned}
$$

REF: Page 91 OBJ: 2-1.2 Solving Equations with the Distributive Property
11. ANS: D

$$
\begin{aligned}
2(24-6 y) & =-48 & & \\
48-12 y & =-48 & & \text { Distribute } 2 . \\
-12 y & =-96 & & \text { Add }-48 \text { to both sides. } \\
y & =8 & & \text { Divide by }-12 .
\end{aligned}
$$

REF: Page 91 OBJ: 2-1.2 Solving Equations with the Distributive Property
12. ANS: D

First, collect all variable terms on one side and all constant terms on the other side. Then, isolate the variable.
REF: Page 92 OBJ: 2-1.3 Solving Equations with Variables on Both Sides
13. ANS: A

First, collect all variable terms on one side and all constant terms on the other side. Then, isolate the variable.
REF: Page 92 OBJ: 2-1.3 Solving Equations with Variables on Both Sides
14. ANS: A

To isolate the variable, first undo the addition or subtraction. Then, undo the multiplication by dividing each side of the inequality by the coefficient of the variable. If the coefficient is negative, reverse the inequality symbol. Next, graph the solution.

Remember, a " $>$ " or " $<$ " graph has an open circle at that value. A " $\geq$ " or " $\leq$ " graph has a closed circle at that value.

A " $>$ " or " $\geq$ " graph has an arrow to the right, and a " $<$ " or " $\leq$ " graph has an arrow to the left.
REF: Page 93 OBJ: 2-1.5 Solving Inequalities
15. ANS: B

To isolate the variable, first undo the addition or subtraction. Then, undo the multiplication by dividing each side of the inequality by the coefficient of the variable. If the coefficient is negative, reverse the inequality symbol. Next, graph the solution.

Remember, a " $>$ " or "<" graph has an open circle at that value. A " $\geq$ " or " $\leq$ " graph has a closed circle at that value.

A " $>$ " or " $\geq$ " graph has an arrow to the right, and a " $<$ " or " $\leq$ " graph has an arrow to the left.
REF: Page 93 OBJ: 2-1.5 Solving Inequalities
16. ANS: A
$3(6-4 x)<-4(3 x-6)$
$18-12 x<-12 x+24 \quad$ Use the Distributive Property.
$0 x<6 \quad$ Isolate $x$. Then simplify.
$0<6 \quad$ Identity.
The solution set is the set of all real numbers.

17. ANS: D
$6(3+4 x)<4(6 x-2)$
$18+24 x<24 x-8 \quad$ Use the Distributive Property.
$0 x<-26 \quad$ Isolate $x$. Then simplify.
$0<-26$
Contradiction.
The inequality has no solution. The solution set is the empty set.

18. ANS: A
$5|x+4|=15$
$|x+4|=3 \quad$ Isolate the absolute-value expression by dividing both sides by 5 .
$x+4=3$ or $x+4=-3 \quad$ Rewrite the absolute value as a disjunction.
$x=-1$ or $x=-7 \quad$ Subtract 4 from both sides of each equation.

REF: Page 152 OBJ: 2-8.2 Solving Absolute-Value Equations
19. ANS: A
$9|x-7|=45$
$|x-7|=5 \quad$ Isolate the absolute-value expression by dividing both sides by 9 .
$x-7=5$ or $x-7=-5 \quad$ Rewrite the absolute value as a disjunction.
$x=12$ or $x=2 \quad$ Add 7 to both sides of each equation.

REF: Page 152 OBJ: 2-8.2 Solving Absolute-Value Equations
20. ANS: B
$\frac{|x-8|}{2} \leq 4 \quad$ Multiply both sides by 2.
$|x-8| \leq 8 \quad$ Rewrite the absolute value as a conjunction.
$x-8 \leq 8$ and $x-8 \geq-8 \quad$ Simplify.
$x \leq 16$ and $x \geq 0$
Graph the solution on a number line. As the inequality symbols include equality, circles should be filled in at the limits indicated by each expression. "Greater than" means values larger than a limit will be included. "Less than" indicates values less than the limit will be included. If there are no solutions that satisfy both inequalities, there is no solution. If all values satisfy the requirements, the solution includes all real umbers.

REF: Page 153 OBJ: 2-8.4 Solving Absolute-Value Inequalities with Conjunctions
21. ANS: A

| $\frac{\|x-14\|}{3} \leq 5$ | Multiply both sides by 3. |
| :--- | :--- |
| $\|x-14\| \leq 15$ | Rewrite the absolute value as a conjunction. |
| $x-14 \leq 15$ and $x-14 \geq-15$ | Simplify. |
| $x \leq 29$ and $x \geq-1$ |  |

Graph the solution on a number line. As the inequality symbols include equality, circles should be filled in at the limits indicated by each expression. "Greater than" means values larger than a limit will be included. "Less than" indicates values less than the limit will be included. If there are no solutions that satisfy both inequalities, there is no solution. If all values satisfy the requirements, the solution includes all real umbers.

## REF: Page 153 OBJ: 2-8.4 Solving Absolute-Value Inequalities with Conjunctions

22. ANS: A

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23. ANS: B

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24. ANS: C

Rewrite the absolute value as a disjunction. Then subtract 6 from both sides and divide by 3 .

$$
\begin{array}{ccc}
|6+3 x|>15 & & \\
6+3 x>15 & \text { or } & 6+3 x<-15 \\
3 x>9 & \text { or } & 3 x<-21 \\
x>3 & \text { or } & x<-7
\end{array}
$$

REF: Page 152 OBJ: 2-8.3 Solving Absolute-Value Inequalities with Disjunctions

